

# Performance Analysis of Economic load Dispatch using Genetic Algorithm

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**Abstract**-Economic Load Dispatch (ELD) is one of the important subjects of concern in power system operation and planning. The main objective of the ELD problems is to present the optimised combination of power outputs of all generating units so as to meet the objective function while taking care of constraints. In conventional computation, the cost function for each unit in ELD problems is solved using mathematical or analytical methods. Generally, these mathematical methods require some marginal cost information to find the global optimal solution. But the fact is that, the real-world input/output characteristics of generating units are highly nonlinear and non-smooth because of prohibited operating zones, valve point loadings, and multi-fuel effects, etc. Thus, the actual ELD problem is represented as a non linear (non smooth) optimization problem having both equality and inequality constraints, cannot be directly solved by conventional analytical techniques. After the evolution of diversified application of soft computing techniques in order to solve these non-smooth ELD problems, many salient methods have been successfully implemented such as hierarchical numerical method, genetic algorithm, evolutionary programming, neural network approaches, differential evolution, particle swarm optimization, and other hybrid method. Genetic algorithm is proved to be efficient optimization techniques over the past few years. In this paper we have presented the solution of an economic load dispatch problem of thermal generator using Genetic Algorithm (GA) method. The proposed method has been implemented on 3 generator system and 6 generator systems. The system considered here is the lossless system. The results obtained show significant improvement in generator fuel cost as compared to conventional techniques while satisfying various equality and inequality constraints.

**Index Terms**-Economic Load Dispatch, Genetic Algorithm, conventional techniques

## 1. INTRODUCTION

Economic Load Dispatch (ELD) is a tool to schedule the generating unit outputs with respect to the specified load demands, so as to operate the power system most economically, or in other words, the main objective of economic load dispatch is optimal allocation of various generating units at the lowest operating cost possible while meeting all system constraints. In recent decade, many efforts have been made to solve the ELD problem, incorporating different kinds of constraints or multiple objectives through various mathematical programming and optimization techniques. The conventional methods include Newton- Raphson method, Lambda Iteration method, Base Point and Participation Factor method, Gradient method, etc [1]. However, these classical dispatch algorithms require the incremental cost curves to be monotonically increasing or piece-wise linear [2]. The input/output characteristics of modern units are inherently highly nonlinear (with valve-point effect, rate limits etc) and having multiple local minimum points in the cost function. Their characteristics are approximated to meet the requirements of classical dispatch algorithms leading to suboptimal solutions and therefore, resulting in huge revenue loss over the time. Consideration of highly nonlinear characteristics

of the units requires highly robust algorithms to avoid getting stuck at local optima [3]. The classical calculus

based techniques fail in solving these types of problems as the problem is non linear. In this respect, stochastic search algorithms like genetic algorithm (GA) [4]-[9], evolutionary strategy (ES) [10]-[12], evolutionary programming (EP) [13], particle swarm optimization (PSO) [14] and simulated annealing (SA) may prove to be very efficient in solving highly nonlinear ELD problem without any restrictions on the shape of the cost curves.

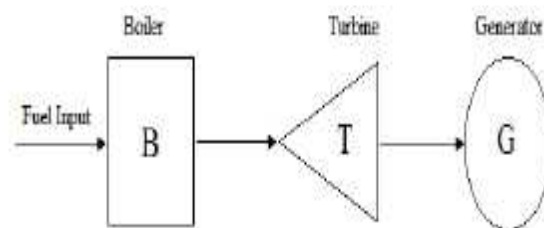


Figure 1. Model of Operation of Fossil Power Plant

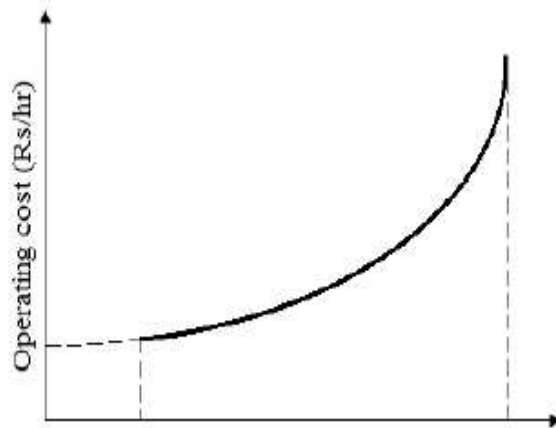


Figure 2. Standard Operating Cost Curve

In figure 1. We have shown the model of a fossil plant showing the fuel input to boiler. The cost of operation is generally approximated by one or more quadratic segments, figure 2. Illustrates the standard operating cost curve of a power plant.

## 2. METHODOLOGY

The applied methodology involves two important -

1. Synthesis of ELD Problem.
2. Application of Genetic Algorithm for optimization.
3. Implementation of Genetic Algorithm in ELD Problem

### 2.1 SYNTHESIS OF ELD PROBLEM

#### 2.1.1 Objective Function (Minimum Cost Function)

The goal of the economic dispatch problem is to minimize the total fuel cost of generating units while satisfying the equality and inequality constraints of given generating system. The simplified cost function of each generator can be presented by a quadratic function shown in given

$$F(P_{gi}) = \sum_{i=1}^{NG} F_i(P_{gi})$$

$$F_i(P_{gi}) = a_i P_{gi}^2 + b_i P_{gi} + c_i \text{ Rs/hr}$$

expression

.....(i)

..... (ii)

In this expression  $a_i$ ,  $b_i$ ,  $c_i$  are cost coefficients for  $i$ th unit,  $F_i(P_{gi})$  is the total cost of generation,  $P_{gi}$  is the generation of  $i$ th plant. In order to balance the power, an equality constraint should be satisfied. The total generated power should be equal to the sum of total load demand and total transmission line loss.

$$\sum P_{gi} = P_D + P_{\text{loss}} \text{ .....(iii)}$$

Such that  $P_D$  is the total demand and  $P_{\text{loss}}$  is total loss.

#### 2.1.2. Constraints-

Power output of each generating unit (generator) should have value of generation in between maximum

and minimum limits of their generating capacity. The corresponding inequality constraints for each generator lie between these two values.[6]

### 2.2 Application of Genetic Algorithm for optimization

Genetic Algorithm (GA) is a soft computing technique used in to find exact or approximate solutions to optimization and search problems. Genetic algorithms are categorized as global search heuristics. Genetic algorithms come under class of Evolutionary Algorithms (EA) that use techniques inspired by evolutionary biology such as inheritance, mutation, selection, and crossover.

Genetic algorithms are processed as a simulation tool in which a population of abstract termed as chromosomes or the genotype of the genome of candidate solutions termed as individuals, creatures, or phenotypes to an optimization problem evolves toward better solutions.[5]

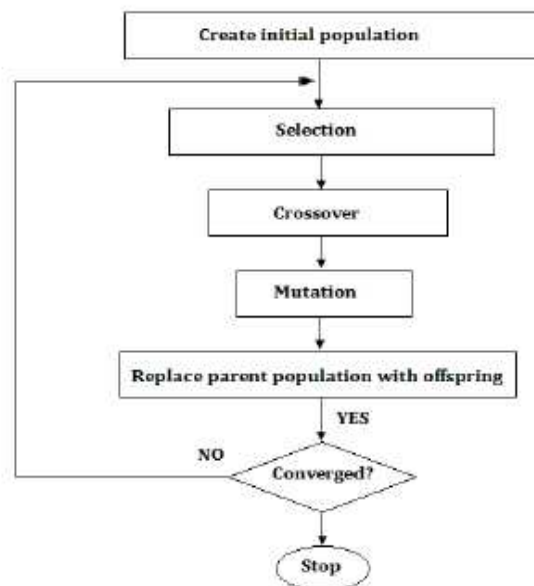


Figure 3. Flowchart of operation of GA

Figure 3 shows the flow chart of operation of GA whose constituents block and their operations are explained as follows.

#### 2.2.1 Representation

In genetic algorithm all solution of a problem corresponds to chromosome whereas the set of solutions or set of chromosomes forms a population or search space.

#### 2.2.2 Encoding

A chromosome links to a unique solution in the solution search space. This requires a mapping formulation between the search space (population) and the chromosomes. This mapping is called an encoding. In fact, GA works on the *encoding* of a problem, not on the problem itself. Encoding is the initial stage of operation of Genetic Algorithm.[7]

### 2.2.3 Decoding

Decoding is the process of conversion of the encoded value of chromosomes into decimal equivalents of the feature values. The decoded feature values are meant to calculate the important problem performance parameters like the objective function, fitness values, constraint violation and system statistical characteristics like variance, standard deviation and rate of convergence.

### 2.2.4 Initialization

Initially many individual solutions are randomly generated to form an initial population. The population size depends on the nature of the problem, but typically contains several hundreds or thousands of possible solutions. Traditionally, the population is generated randomly, covering the entire range of possible solutions (the *search space*).

### 2.2.5 Evaluation

Efficiency and effectiveness of the solutions is calculated from the initial set of solution of the problem. For this effectiveness calculation, we use a function called fitness function. This function is derived from the objective function and used in successive genetic operation. The evaluation function is a procedure for establishing the fitness of each chromosome in the population and is very much application orientated.[10]

### 2.2.6 Fitness Function (Objective Function)

The function calculating the output or objective is called fitness function and the measure of effectiveness is given by fitness value of particular solution. This principal is used to find fitness value of the process for solving maximization problems. Minimization problems are usually transferred into maximization problems using some suitable transformations.

### 2.2.7 Selection

During each successive generation, a proportion of the existing population is selected to breed a new generation. Individual solutions are selected through a *fitness-based* process, where fitter solutions (as measured by a fitness function) are typically more likely to be selected.

### 2.2.8 Crossover-

Two best chromosomes from a given population are reproduced to form new offspring; this process is defined as crossover. There are several types of crossover, in our problem we have used one point crossover with given crossover probability  $P_c$  of

### 2.2.9 Mutation

Mutation is done inside new offspring to enhance the fitness value and make the solution more efficient. In our problem the probability of mutation  $P_m$  is taken as

This generational process is repeated until a termination condition has been reached. Common terminating conditions are:[11]

1. Minimum criteria solution is achieved.
2. Set number of generations has been reached
3. Computation time/money reached
4. The highest ranking solution's fitness is reaching or has reached a plateau such that successive iterations no longer produce better results
5. Manual inspection
6. Combinations of the above.

## 2.3. Implementation of Genetic Algorithm in ELD Problem

The given 3 generator problem has been taken from Haddisaddat Power system book example 7.8.

### Case-1. 3 Generator Systems

Given data-The cost function is given as

Cost = [200 7.0 0.008; 180 6.3 0.009; 140 6.8 0.007];

The generating limit is given as

MW limits = [10 85; 10 80; 10 70];

The demand in Mega Watt is given as (variable)

$P_{dt} = 150$ ;

The loss matrix is given as

$B = [0.0218 \ 0.0093 \ 0.0028; 0.0093 \ 0.0228 \ 0.0017$

$; 0.0028 \ 0.0017 \ 0.0179]$ ;

$B_0 = [0.0003 \ 0.0031 \ 0.0015]$ ;

$B_{00} = 0.00030523$ ;

The base value of mva is taken as

Base mva = 100;

### Case-2. 6 Generator Systems

The data matrix should have 5 columns of fuel cost coefficients and plant limits.

- |                          |                    |         |
|--------------------------|--------------------|---------|
| 1. (\$/MW <sup>2</sup> ) | 2. \$/MW           | 3. (\$) |
| 4. Lower limit(MW)       | 5. Upper limit(MW) |         |

data = [0.007 7 240 100 500

0.0095 10200 50200

0.009 8.5 220 80300

0.009 11200 50150

0.008 10.5 220 50200

0.0075 12120 50120];

Here number of rows denote the number of plants (n).

The loss matrix is given as

$B = 1e-4 * [0.14 \ 0.17 \ 0.15 \ 0.19 \ 0.26 \ 0.22$

$0.17 \ 0.6 \ 0.13 \ 0.16 \ 0.15 \ 0.2$

$0.15 \ 0.13 \ 0.65 \ 0.17 \ 0.24 \ 0.19$

$0.19 \ 0.16 \ 0.17 \ 0.71 \ 0.3 \ 0.25$

$0.26 \ 0.15 \ 0.24 \ 0.3 \ 0.69 \ 0.32$

$0.22 \ 0.2 \ 0.19 \ 0.25 \ 0.32 \ 0.85$

];

The demand in Mega Watt is given as (variable)

$P_d=700$ ;

The step-wise procedure is outlined below:

1. Get data, cost coefficients,  $a_i$ ,  $b_i$ ,  $c_i$ , no. of iterations, length of string, population size, probability of crossover and mutations, power demand,  $P^{\min}$  and  $P^{\max}$ .
2. Create the initial population randomly using binary encoding.
3. Decode the string, or obtain the decimal integer from the binary string using given equation-

$$y^j = \sum_{i=1}^I 2^{i-1} b_i^j \quad (j = 1, 2, \dots, L) \quad \dots(iv)$$

4. The Power output from the decoded population is calculated using following equation

$$P_i^j = P_i^{\min} + \frac{P_i^{\max} - P_i^{\min}}{2^j - 1} y_i^j \quad (i = 1, 2, \dots, NG, j = 1, 2, \dots, L) \quad \dots(v)$$

5. Check  $P_i^j$  if  $P_i^j$  is greater than  $P^{\max}$  then set  $P_i^j$  equal to  $P^{\max}$  and if  $P_i^j$  is smaller than  $P^{\max}$  then set  $P_i^j$  equal to  $P^{\min}$ .
6. Find fitness if ( $F_j > F^{\max}$ ) then set  $F^{\max} = F_j$  and if ( $F_j < F^{\max}$ ) then set  $F^{\min} = F_j$ .
7. Find population with maximum fitness and average fitness of the population.
8. Select the parents for crossover using stochastic remainder roulette wheel selection method.
9. Perform single point crossover for the selected parents.
10. Perform mutation.
11. If the number of iterations reaches the maximum, then go to step 12. Otherwise, go to step 2.
12. The fitness that generates the minimum total generation cost is the solution of the problem.

#### 4. RESULTS

The result of ELD after the implementation of proposed GA method is discussed. The Simulation of given data were done in Matlab R2013a. The results of plant allocation and cost of generation was compared with that of conventional analytical method. The coefficients of fuel cost and maximum and minimum power limits are needed to be given. The power demand is considered to be 150 (MW) and 700 (MW) respectively for 3 generator system and 6 generator system. The length of string in the population has been taken as 48 and 96 respectively and the population size has been assumed as 10 and 20 respectively. The single string represents three substrings, each of 16 bits. Therefore, population we have taken is  $10 \times 48$  and  $20 \times 96$  respectively in binary. The mutation probability is taken as 0.1. and crossover probability as 0.9.

The Comparative analysis between conventional and soft computing approach (GA) is shown below-

**Table-1**

No. Of Generators	Power Demand(MW)	Cost (Conventional)	Cost (GA)
3	150	1599.98 \$/h	1597.48 \$/h
6	700	8360.61 \$/h	8352.61 \$/h

The Plant allocation is given as –

#### Case-1. For 3 generator system

**Table-2**

Peak Demand	P1(MW)	P2(MW)	P3(MW)	Gen. Cost(\$/h)
150 MW	32.8101	64.5950	54.9369	1597.4800
200MW	54.1854	80.00	70.00	1994.6866
185MW	44.3779	74.9467	69.2098	1873.2744

#### Case-2. For 6 generator system

**Table-3**

Peak Demand	P1	P2	P3	P4	P5	P6	Gen. Cost(\$/h)
700	323.63	76.685	158.43	50.00	51.97	50.00	8352.6109
750	339.77	88.02	170.06	50.00	64.59	50.00	8949.2093
800	355.99	99.38	181.7274	50.00	77.22	50.00	9558.5647

The results are shown with the help of tabular representation Table 1 shows the comparative analysis of conventional method and GA based approach showing the utility and advantage of using GA in ELD problem.

Table 2 and Table 3 shows the application of GA in plant allocation for optimum generation in various power demand scenario.

#### 5. CONCLUSIONS

The genetic algorithm have successfully implemented for solving the optimization problem if Economic load

dispatch. The results were improved and more efficient as compared to analytical and conventional algorithm. This method is useful for any number of generators and variable power demand as well. Further the result can be enhanced by using hybrid optimization techniques and more real world constraints so as to get optimum and accurate solution.

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